

YEAR 3

MAIN PRINCIPLES

What is maths mastery?

Teaching maths for mastery is a transformational approach to maths teaching which stems from high performing Asian nations such as Singapore. When taught to master maths, children develop their mathematical fluency without resorting to rote learning and are able to solve non-routine maths problems without having to memorise procedures.

Concrete, pictorial, abstract (CPA)

Concrete, pictorial, abstract (CPA) is a highly effective approach to teaching that develops a deep and sustainable understanding of maths. Developed by American psychologist, Jerome Bruner, the CPA approach is essential to maths teaching in Singapore.

Number bonds

Number bonds are a way of showing how numbers can be combined or split up. They are used to reflect the 'part-part-whole' relationship of numbers.

Bar modelling

The bar model method is a strategy used by children to visualise mathematical concepts and solve problems. The method is a way to represent a situation in a word problem, usually using rectangles.

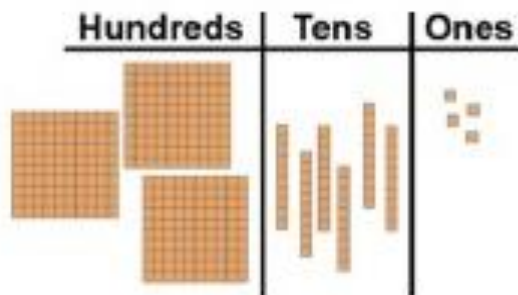
Fractions

In Singapore, the understanding of fractions is rooted in the Concrete, Pictorial, Abstract (CPA) model, where children use paper squares and strips to learn the link between the concrete and the abstract. At the heart of understanding fractions is the ability to understand that we're giving an equal part a name.

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PLACE VALUE

Base ten or dienes blocks:



Value of digits:

| hundreds | tens | ones |
|----------|------|------|
| 4 | 2 | 7 |

$427 = 4 \text{ hundreds} + 2 \text{ tens} + 7 \text{ ones}$
 $427 = 400 + 20 + 7$

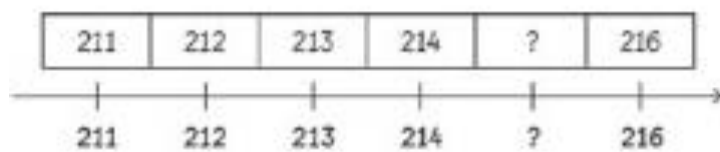
The digit 4 stands for 4 hundreds or 400.

The digit 2 stands for 2 tens or 20.

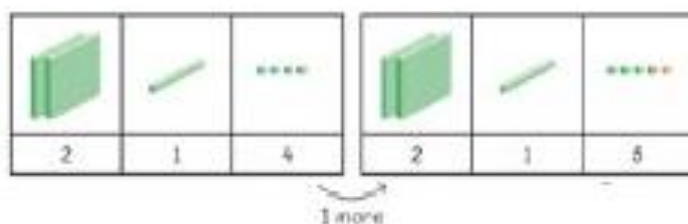
The digit 7 stands for 7 ones or 7.

We write 427 as four hundred and twenty-seven.

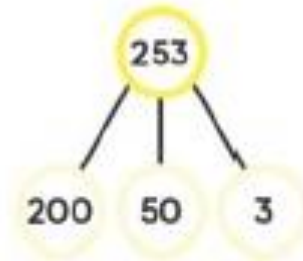
Number lines:



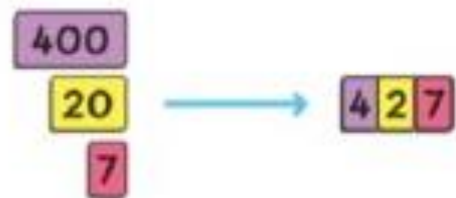
Finding 1 more or less than:



Number bond method:

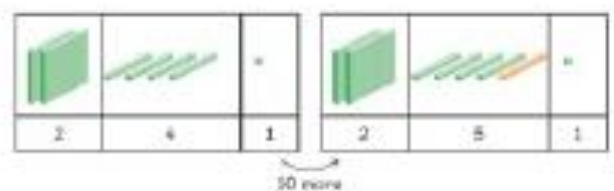


Place value cards:

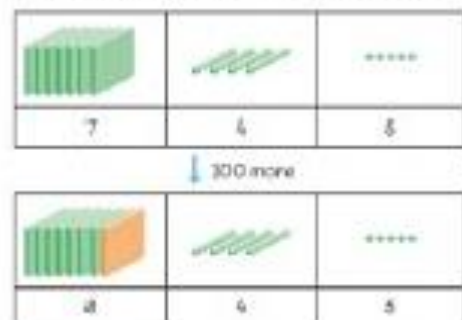


Separating the numbers apart like this is called **partitioning**.

Finding 10 more or less than:



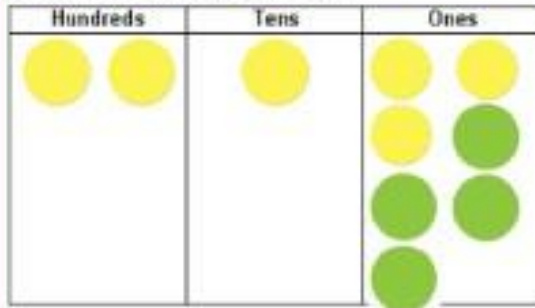
Finding 100 more or less:



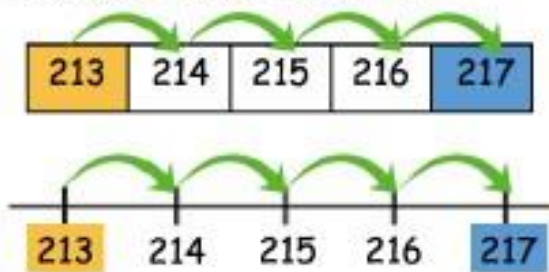
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ADDITION

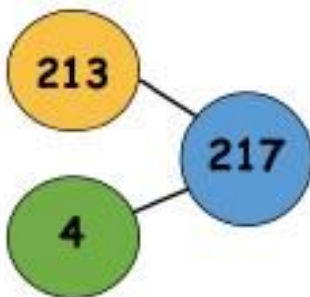
Counters method:



Number line method:



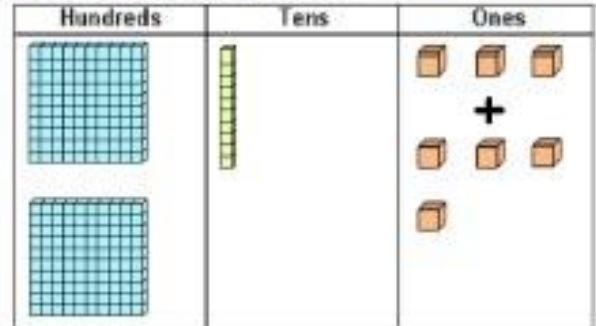
Number bond method:



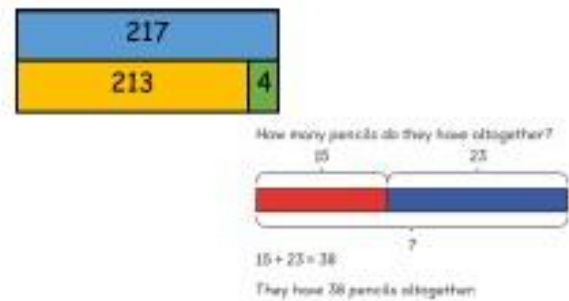
Abstract calculations:

| Commutative | Inverse |
|-----------------|-----------------|
| $213 + 4 = 217$ | $217 - 4 = 213$ |
| $4 + 213 = 217$ | $217 - 213 = 4$ |

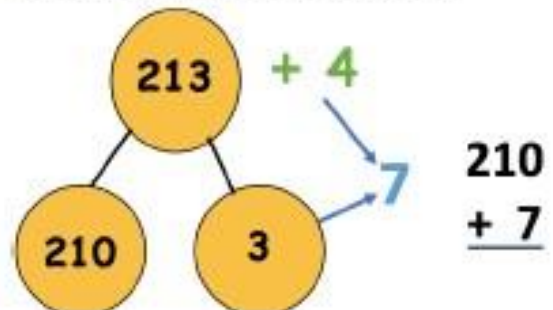
Base 10 method:



Bar model:



Number bond method:



Column addition:

Without renaming:

$$\begin{array}{r} 213 \\ + \quad 4 \\ \hline 217 \end{array}$$

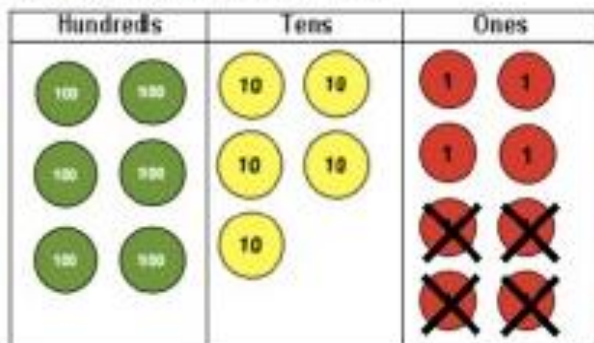
With renaming:

$$\begin{array}{r} 11 \\ 213 \\ + 497 \\ \hline 710 \end{array}$$

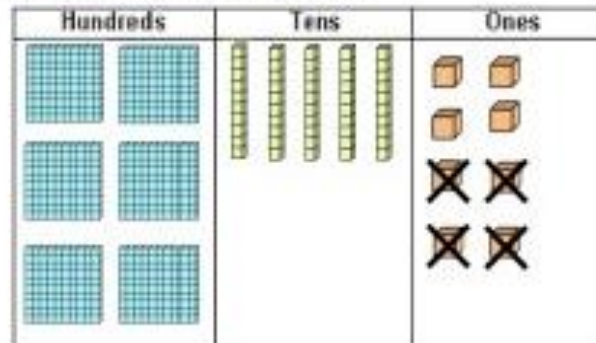
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SUBTRACTION

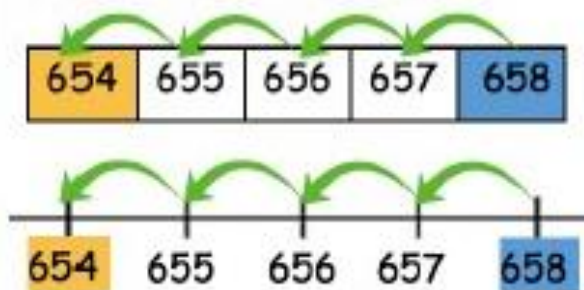
Counters method:



Base 10 method:



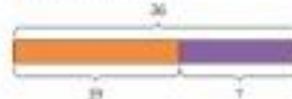
Number line method:



Bar models:

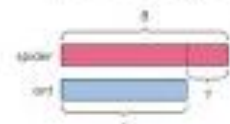
Bar model:

There are 36 children in the school band.
22 of them are boys.
How many girls are there?



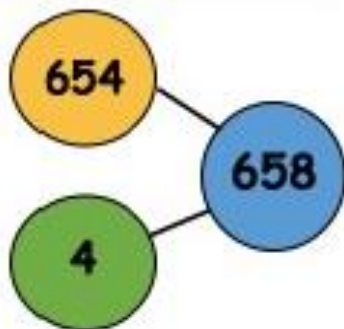
Comparative model:

A spider has 8 legs.
An ant has 6 legs.

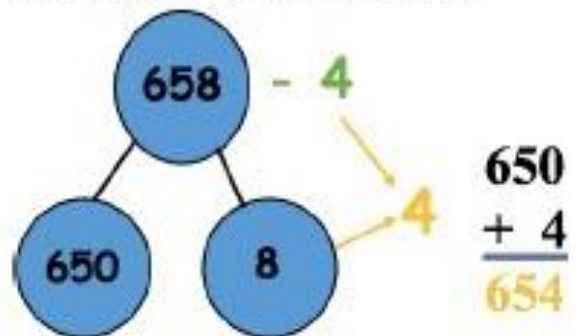


$8 - 6 = 2$
A spider has 2 more legs than an ant.

Number bond method:



Number bond method:



Abstract calculations:

| Commutative | Inverse |
|-----------------|-----------------|
| $658 - 4 = 654$ | $654 + 4 = 658$ |
| $658 - 654 = 4$ | $4 + 654 = 658$ |

Column subtraction:

Without renaming:

$$\begin{array}{r} 658 \\ - \quad 4 \\ \hline 654 \end{array}$$




With renaming:

$$\begin{array}{r} 6\overset{4}{\cancel{5}}\overset{1}{8} \\ - 349 \\ \hline 309 \end{array}$$


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MULTIPLICATION

Arrays:


| 3 times tables | 4 times tables | 8 times tables |
|---|---|---|
|  |  |  |
| $3 \times 5 = 15$ | $4 \times 5 = 20$ | $8 \times 5 = 40$ <small>(doubling the 4 times tables)</small> |

Make a family of multiplication and division facts:



$6 \times 4 = 24$ $24 \div 6 = 4$
 $4 \times 6 = 24$ $24 \div 4 = 6$

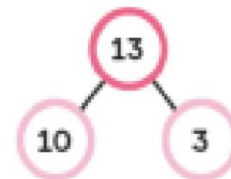
Number bond strategy: Multiplication



$12 \times 4 = 48$
 $10 \times 4 = 40$ $2 \times 4 = 8$

Bridged column method: Without renaming

$13 \times 3 = 39$



| | | |
|---|---|---|
| | t | o |
| | 1 | 3 |
| x | | 3 |
| | | 9 |
| + | 3 | 0 |
| | 3 | 9 |

Bridged column method: With renaming

Multiply the ones by 4.

| | | |
|---|---|---|
| | t | o |
| | 2 | 5 |
| x | | 4 |
| | 2 | 0 |

5 ones $\times 4 = 20$ ones
20 ones = 2 tens

Multiply the tens by 4.

| | | |
|---|---|---|
| | t | o |
| | 2 | 5 |
| x | | 4 |
| | 8 | 0 |

2 tens $\times 4 = 8$ tens

Add the products.

| | | | |
|---|---|---|---|
| | h | t | o |
| | | 2 | 5 |
| x | | | 4 |
| | | 2 | 0 |
| + | | 8 | 0 |
| | 1 | 0 | 0 |

20 + 80 = 100

Short multiplication: Without renaming

$2 \times 4 = 8$



$2 \times 40 = 80$



Short multiplication: With renaming

Multiply the ones by 4.

| | | | |
|---|--------|---|---|
| | 2 tens | t | o |
| | | 2 | 7 |
| x | | | 4 |
| | | | 8 |

8 ones

7 ones $\times 4 = 28$ ones
28 ones = 2 tens + 8 ones

Multiply the tens by 4.

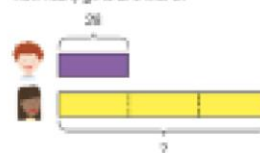
| | | | |
|---|---|---|---|
| | h | t | o |
| | | 2 | 7 |
| x | | | 4 |
| | 1 | 8 | 8 |

4 tens $\times 4 = 16$ tens
16 tens + 2 tens = 18 tens

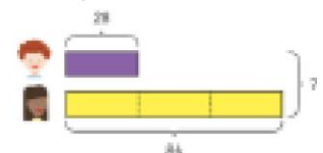
Solving word problems: Bar model

There are 28 boys in a group.
There are 3 times as many girls as there are boys.

(a) How many girls are there?



(b) How many children are there?



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DIVISION

Grouping: 'groups of'

Put 8 🍪 into groups of 4.



$$8 \div 4 = 2$$

2 plates are needed.

"I have made groups of 4. There are 2 equal groups. There are 4 in each group. 2 equal groups of 4 equals 8."

Grouping: 'equal groups'

Put 8 🍪 into 4 equal groups.



$$8 \div 2 = 4$$

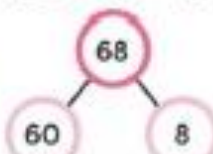
4 trays are needed.

"There are 4 equal groups. There are 2 in each group. 4 equal groups of 2 equals 8."

Number bond strategy: Division

6 tens \div 2
= 3 tens

$$68 \div 2 = 34$$



8 ones \div 2
= 4 ones



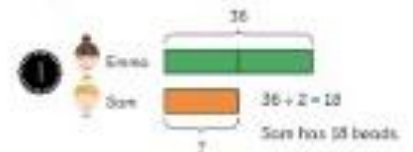
6 tens \div 2

8 ones \div 2



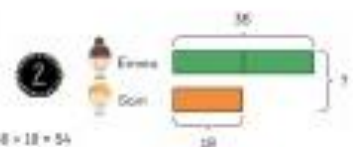
Solving word problems: Bar model

How many beads do the children have altogether?



Emma has 36 beads.

She has twice as many beads as I have.



Make a family of multiplication and division facts:



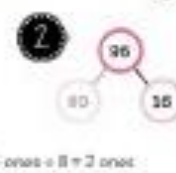
$$6 \times 4 = 24 \quad \text{---} \quad 24 \div 6 = 4$$

$$4 \times 6 = 24 \quad \text{---} \quad 24 \div 4 = 6$$

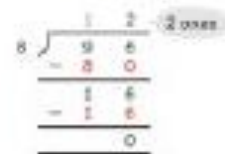
Number bond and long division:



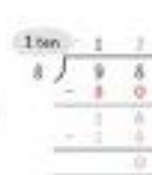
First, I take 80 from 96. Then, I take 16 from the remaining 16.



16 ones \div 8 = 2 ones



8 tens \div 8 = 1 ten



1 ten \div 2 ones = 12

96 \div 8 = 12